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## Microprogram Automation: Design for Testability

A. Keevallik, M. Kruus, H. Lensen

*Department of Computer Engineering, TTU, Ehitajate tee 5, EE0026 Tallinn, Estonia,  
e-mail: kruus@cc.ttu.ee hl@cc.ttu.ee*

**ABSTRACT:** In this work we present a Checking Sequence design method for Finite State Machines (FSM). Microprogram Automation (MPA) model is used to describe source FSM. Testability of MPA is improved by introducing additional binary inputs or outputs. This modification enhances indirect observability of MPA States and allows to compose universal Checking Sequences for such redundant Automations using an algorithm described in this paper. Generated checking sequence is independent of MPA hardware implementation. The introduced method is applied on several MCNC Benchmark Automation examples and a short overview of experimental results is listed.

### 1 Introductions

For a long time the formalized methods for digital control systems logical design, based on finite automata theory, were not widely used in practical design. The main reason was the high combinatorial complexity of optimization tasks. Most of the modern formalized methods for digital control units design use the Finite State Machine (FSM) model to describe the source unit. The test methods, based on checking experiments theory [1,2] are not often used because of the high upper bound of checking sequence length.

In this paper, we propose to use so-called microprogram automaton (MPA) model [3] to compose an universal checking sequence independent of FSM implementation. It is shown that composed sequence enables to check all the observed faults in MPA. A testable design method is proposed to guarantee the existence of distinguishing sequence [1,2] for MPA.

### 2 Basic Notations

Our basic research object is regarded as Microprogram Automaton (MPA). This model is similar to the ordinary initial FSM model, but includes sets of binary vectors as input and output alphabets.

Microprogram Automaton  $A$  is defined [3] as

system  $A = \left( \{0,1\}^L, S, \{0,1\}^M, \delta, \lambda, s_0 \right)$ , where

$\{0,1\}^L$  is input alphabet,  $L$  - the number of binary inputs;

$S$  - set of internal states,  $|S| = n$ ;

$\{0,1\}^M$  - output alphabet,  $M$  - the number of binary outputs;

$\delta: S \times \{0,1\}^L \rightarrow S$  - transition function;

$\lambda: S \times \{0,1\}^L \rightarrow \{0,1\}^M$  - output function;

$s_0$  - initial state of MPA.

The input and output vectors are denoted by  $x_1 x_2 \dots x_L$  and  $y_1 y_2 \dots y_M$ , respectively.

MPA  $A$  can be presented by the list of its transitions (Tab.1.), similar to the state and output tables of FSM.

Any row from this list describes one of generalized transitions (G-transitions) of MPA. The set of MPA transitions is determined by the set of generalized input vectors (G-inputs)  $\tilde{x}_1 \tilde{x}_2 \dots \tilde{x}_L$ , where

$\tilde{x}_i \in \left\{ x_i, \bar{x}_i, \times \right\}, 1 \leq i \leq L$  and  $\tilde{x}_i = \times$  denotes that

described G-transition is not dependent of input  $x_i$ . For

any transition of MPA there exist the sets of essential inputs (on which transition and output functions depend) and inessential inputs. For essential inputs

$\tilde{x}_i \in \left\{ x_i, \bar{x}_i \right\}$ , for inessential inputs  $\tilde{x}_i = \times$ . Any row

of transition list describes the set of elementary transitions (E-transitions).

Number of transition	Initial state	Final state	Generalized input vector	Output vector
1	s1	s2	x1	y1y2
2		s2	-x1x2	y1y3
3		s5	-x1-x2	y1y2
4	s2	s1	-x1-x3	y3y4
5		s2	x1-x3	y4
6		s3	x3	y1y2y3
7	s3	s1	-x1-x4	y3y4
8		s2	x1-x4	y3
9		s4	x4	y2y3y4
10	s4	s1	x3	y1
11		s2	-x3	y4
12	s5	s4	1	y3y4

**Table 1. Transition list of MPA A**

For example, G-transition in row 7 describes four E-transitions from state  $s_3$  to state  $s_1$  under input vectors 0000, 0010, 0100, 0110. For this generalized transition  $\{x_1, x_4\}$  and  $\{x_2, x_3\}$  are the sets of essential and inessential inputs. The number of generalized transitions in the list is denoted as  $H$ .

### 3 Distinguishing sequence design for MPA

Our approach is based on the checking experiments theory [1,2], but some useful properties of MPA model give us possibility to find a short DS in the most of cases.

Let  $p = X_1 X_2 \dots X_k, X_i \in \{0,1\}^L$  be a sequence of input vectors. Length of sequence  $p$  is denoted by  $d(p)$ . The set of finite length input and output sequences is denoted by  $\left\{ \{0,1\}^L \right\}^*$  and  $\left\{ \{0,1\}^M \right\}^*$ , respectively.

Function  $\bar{\delta}: S \times \left\{ \{0,1\}^L \right\}^* \rightarrow S$  is said to be a

**generalized transition function** of MPA  $A$ .  $\bar{\delta}(s, p)$  defines the final state of MPA if input sequence  $p$  is applied in the initial state  $s$ .

Function  $\bar{\lambda}: S \times \left\{ \{0,1\}^L \right\}^* \rightarrow \left\{ \{0,1\}^M \right\}^*$  is said to

be a **generalized output function** of MPA  $A$  and  $\bar{\lambda}(s, p)$  defines the output sequence if input sequence  $p$  is applied in the initial state  $s$ .

Input sequence  $p$  is said to be **the distinguishing sequence** [1] ( $DS$ ) for MPA  $A$ , iff for any pair of states

$$s, t \in S \quad \bar{\lambda}(s, p) = \bar{\lambda}(t, p) \Leftrightarrow s = t.$$

In the following, MPA  $A$  is regarded as **k-testable** iff there exist the  $DS$  for MPA  $A$  and  $d(DS)=k$ .

In common case the checking sequence  $\alpha$  for FSM  $A$  can be constructed by the Hennie's method [1] and it must check all transitions of FSM  $A$  (by applying  $DS$  after any transition under check).

Small redundancy of MPA outputs enables us to avoid the high complexity algorithms for  $DS$  design [1,2], based usually on investigation of FSMs successor tree.

Let us denote by  $g(i)$ ,  $1 \leq i \leq H$ , the number of E-transitions described by G-transition in row  $i$  and by  $U$  the set of all G-transitions of MPA  $A$ . **Following method enables to find  $DS$  for 1-testable MPA  $A$ .**

#### Algorithm 1

1.  $i=0, k=1$
2.  $i=i+1$ ; find the set  $W \subset U$  of G-transitions from states  $s_{k+1}, \dots, s_n$ , which have a similar output vector with generalized transition  $i$ .
3. **If**  $W \neq \emptyset$  **then** include G-transition  $i$  into  $W$ ; select the transition  $w \in W$ , which have greatest value  $g(w)$  in the set  $W$ ; ban G-inputs of other G-transitions from set  $W$  as  $DS$ ;  $U = U \setminus W$ .
4. **If** there are no more G-transitions from state  $k$ , **then**  $k=k+1$ .
5. **If**  $k < n$ , **then** goto 2.
6. End.

As a result of proposed algorithm we get the set of input vectors each of which can be used as a  $DS$  for observed MPA. Karnough map is used to describe the steps of algorithm (Tab.2).

x3x4	00	01	11	10
x1x2				
00	r1	r1	<b>DS</b>	r1
01	r1	r1	<b>DS</b>	r1
11	r2	r2	<b>DS</b>	<b>DS</b>
10	r2	r2	<b>DS</b>	<b>DS</b>

**Table 2. Karnough map for  $DS$**

Transitions from state  $s_1$  have not similar output reactions with other states. Consequently, output vectors  $y_1 y_2$  and  $y_1 y_3$  can be used to distinguish state  $s_1$  with no restrictions on input vector. G-transition 4 from state  $s_2$  has similar output reaction with G-transitions 7 and 12. Since transition 12 is unconditional, output reaction  $y_3 y_4$  must be attached to state  $s_5$ . Therefore we have

restrictions on input vector denoted by r1 on Karnough map. G-transition 5 has a similar reaction with G-transition 11. Hence there are four E-transitions described in row 5 and eight E-transitions in row 11, lets ban G-input of transition 5 (restrictions are denoted by r2). Undaged input vectors can be used as  $DS$  for MPA  $A$ . These vectors are denoted by  $DS$  on Karnough map.

The above algorithm fails if the source MPA is not 1-testable. But 1-testability can be achieved by introducing some extra binary inputs or outputs. MPA  $B$  (Tab.3) is not 1-testable (moreover, it also has not longer  $DS$ ), but 1-testability results from introducing an extra input  $x_3$ .

For MPA  $B'$  (Tab.4), where  $\delta(s_i, x_3) = s_i$  and  $\lambda(s_i, x_3)$  gives a unique reaction for any state  $s_i$ , G-input  $x_3$  can be used as  $DS$ . 1-testability of MPA  $B$  can

also be achieved by introducing one extra output ( $y_4$ ) as it is done for MPA B'' (Tab.5). An extra output  $y_4=1$  for G-transitions 2 and 3 and  $y_4=0$  for other G-transitions.

As a result, G-input  $\bar{x}_1$  can be used as a DS. Denote that the number of extra outputs  $z$  may be greater than 1 and in common case it can be estimated as follows:  $z \leq \text{int}(\log_2(|W_{\max}|)) + 1$ , where  $W_{\max}$  is the set  $W$  with maximal power in **algorithm 1**. We assume in following that source MPA is 1-testable.

Number of transition	Initial state	Final state	Generalized input vector	Output vector
1	s1	s2	x1	y1
2		s1	-x1x2	y1y3
3		s3	-x1-x2	y2y3
4	s2	s1	x1	y1
5		s3	-x1	y2y3
6	s3	s2	x2	y1y3
7		s1	-x2	y1

**Table 3. MPA B**

Number of transition	Initial state	Final state	Generalized input vector	Output vector
1	s1	s2	x1-x3	y1
2		s1	-x1x2-x3	y1y3
3		s3	-x1-x2-x3	y2y3
4		s1	x3	y1
5	s2	s1	x1-x3	y1
6		s3	-x1-x3	y2y3
7		s2	x3	y2
8	s3	s2	x2-x3	y1y3
9		s1	-x2-x3	y1
10		s3	x3	y1y2

**Table 4. MPA B'**

Number of transition	Initial state	Final state	Generalized input vector	Output vector
1	s1	s2	x1	y1
2		s1	-x1x2	y1y3y4
3		s3	-x1-x2	y2y3y4
4	s2	s1	x1	y1
5		s3	-x1	y2y3
6	s3	s2	x2	y1y3
7		s1	-x2	y1

**Table 5. MPA B''**

#### 4 Checking sequence design for MPA

The states of FSM are assumed not to be directly observable. According these assumptions, the input sequence  $\alpha$  is said to be the checking sequence, if it passes all states and transitions of FSM (from known initial state) and final state of any transition is checked by

DS. In previous section we reduced the length of DS:  $d(DS)=1$ .

First of all, we will design the checking sequence that enables to pass and check all G-transitions of MPA. Such a sequence is enough easy to compose: it can be build up as some traversal  $\alpha$  of state transition graph (STG) of MPA with DS after any G-transition under check. The initial part of such traversal  $\alpha$  for MPA A (Tab.1) can be composed from initial state s1 as follows:

State	s1	s2	s3	s4	s5	s2 ....
E-input	1011	0011	0011	0011	0111	.....

Note that DS can be chosen from results of **algorithm 1** (Tab.2) and the new G-transition under check can be regarded as DS for previous G-transition if it is possible. Checking sequence  $\alpha$

checks actually one of E-transitions from any G-transitions under check. Inessential inputs of used E-transition are fixed by random way.

Lets introduce the fault classification for MPA. All the faults of MPA can be divided into external and internal faults.

External faults are regarded as permanent faults on MPA inputs and outputs. All external faults are surely detectable by sequence  $\alpha$ .

There can be denoted three main types of internal faults: the faults of output function, faults of the transition function and faults of G-inputs.

The faults of output function are extra or missing faults of binary outputs of some G-transition.

The faults of transition function can be described as the final state faults:  $\delta(s_i, x)$  gives as result the faulty final state. Fault is detectable by applying DS after faulty G-transition and thus can be checked by sequence  $\alpha$ .

Let us return to composed checking sequence  $\alpha$ . Sequence  $\alpha$  was composed as the traversal of STG and includes DS after any checked transition. The G-input faults can be detected if the sequence  $\alpha'$  is concatenated to sequence  $\alpha$ . Sequence  $\alpha'$  includes the second traversal to detect shrinkage G-input faults. Sequence  $\alpha'$  is shorter than sequence  $\alpha$ , since  $\alpha'$  don't include DS after transitions. Note that sequences  $\alpha$  and  $\alpha'$  may be partially covered.

The length of sequence  $\alpha$  has the following upper bound:  $d(\alpha) \leq (n+1) \times H$ , where  $n$  is the number of MPA states and  $H$  is the number of G-transitions of MPA. Each of  $H$  G-transitions must be passed with following DS ( $d(DS)=1$ ) and there is possible that transfer sequence (with length  $\leq (n-1)$ ) is necessary to reach next G-transition under check.

The length of  $\alpha'$  can be estimated:  $d(\alpha') \leq n \times H$ .

The length of concatenation  $\alpha\alpha'$ :  $d(\alpha\alpha') \leq (2n+1) \times H$ . For our first example (Tab.1):

$d(\alpha\alpha') \leq 11 \times 12 = 132$  input vectors. The actual length in our example is 30 input vectors.

The complete checking sequence  $\alpha\alpha'$  can be presented as follows (Table 6). '+' in forth column shows that input vector can be used as DS for MPA A.

Initial state	Input vector	Next state	/DS/
s1	1110	s2	+
s2	1010	s3	+
s3	0011	s4	+
s4	0011	s1	+
s1	0111	s2	+
s2	0111	s3	+
s3	1110	s2	+
s2	1111	s3	+
s3	0110	s1	
s1	0011	s5	+
s5	1111	s4	+
s4	1110	s1	+
s1	1001	s2	
s2	0101	s1	
s1	0111	s2	+
s2	1000	s2	
s2	0011	s3	+
s3	1110	s4	+
s4	0000	s2	
s2	0010	s3	+
s3	0000	s1	
s1	0100	s2	

s2	1101	s2	
s2	0000	s1	
s1	0000	s5	
s5	0000	s4	
s4	1101	s2	
s2	0010	s3	
s3	1000	s2	
s2	0000	s1	

Table 6. CS for MPA A

## 5 Experimental results and conclusions

The proposed methods of checking sequences design are implemented in CAD system DILOS, created in Department of Computer Engineering by Tallinn Technical University. Experimental results on MCNC benchmarks showed that the most of real complexity digital control units have the short distinguishing sequence, but 65% of observed examples were not 1-testable. The extra output or input introducing is used for these cases.

The experimental researches showed also that real checking sequences are essentially shorter than the upper bound shows and their length is 15...60 % of the estimated upper bound. Some experimental results are illustrated in Table 8.

FSM	Initial Inputs	Initial Outputs	States	Extra Inputs or Extra Outputs	CS upper bound	CS actual length
<i>lion</i>	2	3	4	0	55	27
<i>train11</i>	2	1	11	+2 Outputs	300	124
<i>mark1</i>	5	16	15	0	352	149
<i>beecount</i>	3	4	7	+2 Outputs	224	113
<i>beecount</i>	3	4	7	+1 Input	280	127
<i>tav</i>	4	4	4	+1 Input	265	175
<i>tav</i>	4	4	4	+2 Outputs	245	126
<i>ex1</i>	9	19	20	+1 Output	2898	926
<i>ex4</i>	6	9	14	+1 Output	315	160

Table 8. Experimental results

## References

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